

# CHAPTER 7 (Odd)

1. a. series:  $E, R_1$  and  $R_4$   
parallel:  $R_2$  and  $R_3$
- b. series:  $E$  and  $R_1$   
parallel:  $R_2$  and  $R_3$
- c. series:  $E, R_1$  and  $R_5$ ;  
 $R_3$  and  $R_4$   
parallel: none
- d. series:  $R_6$  and  $R_7$   
parallel:  $E, R_1$  and  $R_4$ ;  
 $R_2$  and  $R_5$
3. a. yes (KCL)
- b.  $I_2 = I - I_1 = 5 \text{ A} - 2 \text{ A} = 3 \text{ A}$
- c. yes (KCL)
- d.  $V_2 = E - V_1 = 10 \text{ V} - 6 \text{ V} = 4 \text{ V}$
- e.  $R_T = R_1 \parallel R_2 + R_3 \parallel R_4 = 2 \Omega \parallel 3 \Omega + 1 \Omega \parallel 4 \Omega = \frac{6}{5} \Omega + \frac{4}{5} \Omega = \frac{10}{5} \Omega = 2 \Omega$
- f.  $I = \frac{E}{R_T} = \frac{10 \text{ V}}{2 \Omega} = 5 \text{ A}$
- g.  $P_{\text{del}} = EI = (10 \text{ V})(5 \text{ A}) = 50 \text{ W}$   
 $V_1 = I(R_1 \parallel R_2) = 5 \text{ A} \left[ \frac{6}{5} \Omega \right] = 6 \text{ V}$   
 $P_1 = \frac{V_1^2}{R_1} = \frac{(6 \text{ V})^2}{3 \Omega} = 12 \text{ W}$   
 $P_2 = \frac{V_1^2}{R_2} = \frac{(6 \text{ V})^2}{2 \Omega} = 18 \text{ W}$
5. a.  $R' = R_1 \parallel R_2 = 10 \Omega \parallel 15 \Omega = 6 \Omega$   
 $R_T = R' \parallel (R_3 + R_4) = 6 \Omega \parallel 12 \Omega = 4 \Omega$
- b.  $I_s = \frac{E}{R_T} = \frac{36 \text{ V}}{4 \Omega} = 9 \text{ A}, I_1 = \frac{E}{R'} = \frac{36 \text{ V}}{6 \Omega} = 6 \text{ A}$   
 $I_2 = \frac{E}{R_3 + R_4} = \frac{36 \text{ V}}{12 \Omega} = 3 \text{ A}$
- c.  $V_a = I_2 R_4 = (3 \text{ A})(2 \Omega) = 6 \text{ V}$
7. a, b.  $I_1 = \frac{24 \text{ V}}{4 \Omega} = 6 \text{ A} \downarrow, I_3 = \frac{8 \text{ V}}{10 \Omega} = 0.8 \text{ A} \uparrow$   
 $I_2 = \frac{24 \text{ V} + 8 \text{ V}}{2 \Omega} = \frac{32 \text{ V}}{2 \Omega} = 16 \text{ A}$   
 $I = I_1 + I_2 = 6 \text{ A} + 16 \text{ A} = 22 \text{ A} \downarrow$
9. a.  $I_1 = \frac{E}{R_1 + R_4 \parallel (R_2 + R_3 \parallel R_5)} = \frac{20 \text{ V}}{3 \Omega + 3 \Omega \parallel (3 \Omega + 6 \Omega \parallel 6 \Omega)}$   
 $= \frac{20 \text{ V}}{3 \Omega + 3 \Omega \parallel (3 \Omega + 3 \Omega)} = \frac{20 \text{ V}}{3 \Omega + 3 \Omega \parallel 6 \Omega} = \frac{20 \text{ V}}{3 \Omega + 2 \Omega}$   
 $= 4 \text{ A}$

- b. CDR:  $I_2 = \frac{R_4(I_1)}{R_4 + R_2 + R_3 \parallel R_5} = \frac{3 \Omega(4 \text{ A})}{3 \Omega + 3 \Omega + 6 \Omega \parallel 6 \Omega}$   
 $= \frac{12 \text{ A}}{6 + 3} = 1.333 \text{ A}$   
 $I_3 = \frac{I_2}{2} = 0.6665 \text{ A}$
- c.  $I_4 = I_1 - I_2 = 4 \text{ A} - 1.333 \text{ A} = 2.667 \text{ A}$   
 $V_a = I_4 R_4 = (2.667 \text{ A})(3 \Omega) = 8 \text{ V}$   
 $V_b = I_3 R_3 = (0.6665 \text{ A})(6 \Omega) = 4 \text{ V}$
11. a.  $R' = R_6 \parallel R_5 \parallel (R_7 + R_8) = 4 \Omega \parallel 8 \Omega \parallel (6 \Omega + 2 \Omega) = 4 \Omega \parallel 8 \Omega \parallel 8 \Omega$   
 $= 4 \Omega \parallel 4 \Omega = 2 \Omega$   
 $R'' = (R_3 + R') \parallel (R_6 + R_9) = (8 \Omega + 2 \Omega) \parallel (6 \Omega + 4 \Omega)$   
 $= 10 \Omega \parallel 10 \Omega = 5 \Omega$   
 $R_T = R_1 \parallel (R_2 + R'') = 10 \Omega \parallel (5 \Omega + 5 \Omega) = 10 \Omega \parallel 10 \Omega = 5 \Omega$   
 $I = \frac{E}{R_T} = \frac{80 \text{ V}}{5 \Omega} = 16 \text{ A}$
- b.  $I_{R_2} = \frac{I}{2} = \frac{16 \text{ A}}{2} = 8 \text{ A}$   
 $I_3 = I_9 = \frac{8 \text{ A}}{2} = 4 \text{ A}$
- c.  $I_{8\Omega} = \frac{(R_6 \parallel R_5)(I_3)}{(R_6 \parallel R_5) + (R_7 + R_8)}$   
 $= \frac{(4 \Omega \parallel 8 \Omega)(4 \text{ A})}{(4 \Omega \parallel 8 \Omega) + (6 \Omega + 2 \Omega)}$   
 $= \frac{(2.67 \Omega)(4 \text{ A})}{2.67 \Omega + 8 \Omega} = 1 \text{ A}$
- d.  $-I_8 R_8 - V_{ab} + I_9 R_9 = 0$   
 $V_{ab} = I_9 R_9 - I_8 R_8 = (4 \text{ A})(4 \Omega) - (1 \text{ A})(2 \Omega) = 16 \text{ V} - 2 \text{ V} = 14 \text{ V}$
13. a.  $I_G = 0 \therefore V_G = \frac{270 \text{ k}\Omega(16 \text{ V})}{270 \text{ k}\Omega + 2000 \text{ k}\Omega} = 1.9 \text{ V}$   
 $V_G - V_{GS} - V_S = 0$   
 $V_S = V_G - V_{GS} = 1.9 \text{ V} - (-1.75 \text{ V}) = 3.65 \text{ V}$
- b.  $I_1 = I_2 = \frac{16 \text{ V}}{270 \text{ k}\Omega + 2000 \text{ k}\Omega} = 7.05 \mu\text{A}$   
 $I_D = I_S = \frac{V_S}{R_S} = \frac{3.65 \text{ V}}{1.5 \text{ k}\Omega} = 2.433 \text{ mA}$
- c.  $V_{DS} = V_{DD} - I_D R_D - I_S R_S = V_{DD} - I_D(R_D + R_S)$  since  $I_D = I_S$   
 $= 16 \text{ V} - (2.433 \text{ mA})(4 \text{ k}\Omega) = 16 \text{ V} - 9.732 \text{ V} = 6.268 \text{ V}$
- d.  $V_{DD} - I_D R_D - V_{DG} - V_G = 0$   
 $V_{DG} = V_{DD} - I_D R_D - V_G$   
 $= 16 \text{ V} - (2.433 \text{ mA})(2.5 \text{ k}\Omega) - 1.9 \text{ V} = 16 \text{ V} - 6.083 \text{ V} - 1.9 \text{ V} = 8.02 \text{ V}$

$$15. \quad a. \quad I = \frac{E}{R_2 + R_3} = \frac{9 \text{ V}}{7 \Omega + 8 \Omega} = 0.6 \text{ A}$$

$$b. \quad E_1 - V + E_2 = 0 \\ V = E_1 + E_2 = 9 \text{ V} + 19 \text{ V} = 28 \text{ V}$$

$$17. \quad a. \quad R_8 \text{ "shorted out"} \\ R' = R_3 + R_4 \parallel R_5 + R_6 \parallel R_7 \\ = 10 \Omega + 6 \Omega \parallel 6 \Omega + 6 \Omega \parallel 3 \Omega \\ = 10 \Omega + 3 \Omega + 2 \Omega \\ = 15 \Omega$$

$$R_T = R_1 + R_2 \parallel R' \\ = 10 \Omega + 30 \Omega \parallel 15 \Omega = 10 \Omega + 10 \Omega \\ = 20 \Omega$$

$$I = \frac{E}{R_T} = \frac{100 \text{ V}}{20 \Omega} = 5 \text{ A}$$

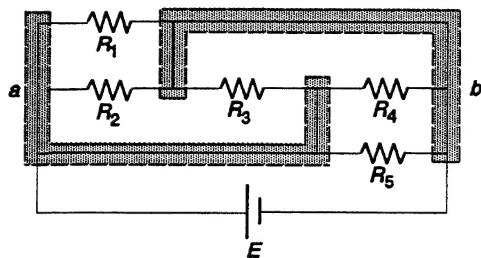
$$I_2 = \frac{R'(I)}{R' + R_2} = \frac{(15 \Omega)(5 \text{ A})}{15 \Omega + 30 \Omega} = 1.667 \text{ A}$$

$$I_3 = I - I_2 = 5 \text{ A} - 1\frac{2}{3} \text{ A} = 3\frac{1}{3} \text{ A}$$

$$I_6 = \frac{R_7 I_3}{R_7 + R_6} = \frac{3 \Omega \left( \frac{10}{3} \text{ A} \right)}{3 \Omega + 6 \Omega} = 1.111 \text{ A} \\ I_8 = 0 \text{ A}$$

$$b. \quad V_4 = I_3(R_4 \parallel R_5) = \left( \frac{10}{3} \text{ A} \right) (3 \Omega) = 10 \text{ V} \\ V_8 = 0 \text{ V}$$

19. a. All resistors in parallel (between terminals a & b)



$$R_T = 16 \Omega \parallel 16 \Omega \parallel 8 \Omega \parallel 4 \Omega \parallel 32 \Omega \\ \quad \quad \quad \underbrace{\quad \quad \quad}_{8 \Omega \parallel 8 \Omega \parallel 4 \Omega \parallel 32 \Omega} \\ \quad \quad \quad \underbrace{\quad \quad \quad}_{4 \Omega \parallel 4 \Omega \parallel 32 \Omega} \\ \quad \quad \quad \underbrace{\quad \quad \quad}_{2 \Omega \parallel 32 \Omega} = 1.882 \Omega$$

- b. All in parallel. Therefore,  $V_1 = V_4 = E = 32 \text{ V}$

c.  $I_3 = V_3/R_3 = 32 \text{ V}/4 \Omega = 8 \text{ A} \leftarrow$

d. 
$$\begin{aligned} I_s &= I_1 + I_2 + I_3 + I_4 + I_5 \\ &= \frac{32 \text{ V}}{16 \Omega} + \frac{32 \text{ V}}{8 \Omega} + \frac{32 \text{ V}}{4 \Omega} + \frac{32 \text{ V}}{32 \Omega} + \frac{32 \text{ V}}{16 \Omega} \\ &= 2 \text{ A} + 4 \text{ A} + 8 \text{ A} + 1 \text{ A} + 2 \text{ A} \\ &= 17 \text{ A} \\ R_T &= \frac{E}{I_s} = \frac{32 \text{ V}}{17 \text{ A}} = 1.882 \Omega \text{ as above} \end{aligned}$$

21. a. Applying Kirchoff's voltage law in the CCW direction in the upper "window":

$$+18 \text{ V} + 20 \text{ V} - V_{8\Omega} = 0$$

$$V_{8\Omega} = 38 \text{ V}$$

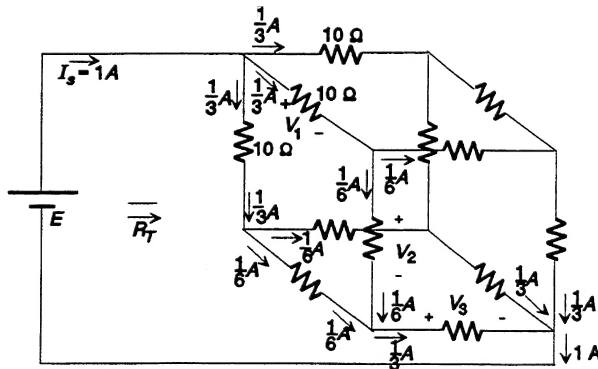
$$I_{8\Omega} = \frac{38 \text{ V}}{8 \Omega} = 4.75 \text{ A}$$

$$I_{3\Omega} = \frac{18 \text{ V}}{3 \Omega + 6 \Omega} = \frac{18 \text{ V}}{9 \Omega} = 2 \text{ A}$$

$$\text{KCL: } I_{18\text{V}} = 4.75 \text{ A} + 2 \text{ A} = 6.75 \text{ A}$$

b.  $V = (I_{3\Omega})(6 \Omega) + 20 \text{ V} = (2 \text{ A})(6 \Omega) + 20 \text{ V} = 12 \text{ V} + 20 \text{ V} = 32 \text{ V}$

23. Assuming  $I_s = 1 \text{ A}$ , the current  $I_s$  will divide as determined by the load appearing in each branch. Since balanced  $I_s$  will split equally between all three branches.



$$V_1 = \left[ \frac{1}{3} \text{ A} \right] (10 \Omega) = \frac{10}{3} \text{ V}$$

$$V_2 = \left[ \frac{1}{6} \text{ A} \right] (10 \Omega) = \frac{10}{6} \text{ V}$$

$$V_3 = \left[ \frac{1}{3} \text{ A} \right] (10 \Omega) = \frac{10}{3} \text{ V}$$

$$E = V_1 + V_2 + V_3 = \frac{10}{3} \text{ V} + \frac{10}{6} \text{ V} + \frac{10}{3} \text{ V} = 8.333 \text{ V}$$

$$R_T = \frac{E}{I} = \frac{8.333 \text{ V}}{1 \text{ A}} = 8.333 \Omega$$

25. a.  $R'_T = R_5 \parallel (R_6 + R_7) = 6 \Omega \parallel 3 \Omega = 2 \Omega$   
 $R''_T = R_3 \parallel (R_4 + R'_T) = 4 \Omega \parallel (2 \Omega + 2 \Omega) = 2 \Omega$   
 $R_T = R_1 + R_2 + R''_T = 3 \Omega + 5 \Omega + 2 \Omega = 10 \Omega$   
 $I = \frac{240 \text{ V}}{10 \Omega} = 24 \text{ A}$

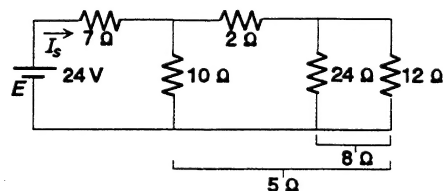
b.  $I_4 = \frac{4 \Omega(I)}{4 \Omega + 4 \Omega} = \frac{4 \Omega(24 \text{ A})}{8 \Omega} = 12 \text{ A}$   
 $I_7 = \frac{6 \Omega(12 \text{ A})}{6 \Omega + 3 \Omega} = \frac{72 \text{ A}}{9} = 8 \text{ A}$

c.  $V_3 = I_3 R_3 = (I - I_4) R_3 = (24 \text{ A} - 12 \text{ A}) 4 \Omega = 48 \text{ V}$   
 $V_5 = I_5 R_5 = (I_4 - I_7) R_5 = (4 \text{ A}) 6 \Omega = 24 \text{ V}$   
 $V_7 = I_7 R_7 = (8 \text{ A}) 2 \Omega = 16 \text{ V}$

d.  $P = I_7^2 R_7 = (8 \text{ A})^2 2 \Omega = 128 \text{ W}$   
 $P = EI = (240 \text{ V})(24 \text{ A}) = 5760 \text{ W}$

27. The  $12 \Omega$  resistors are in parallel.

Network redrawn:



$$R_T = 12 \Omega$$

$$I_s = \frac{E}{R_T} = \frac{24 \text{ V}}{12 \Omega} = 2 \text{ A}$$

$$I_{2\Omega} = \frac{I_s}{2} = \frac{2 \text{ A}}{2} = 1 \text{ A}$$

$$I_{12\Omega} = \frac{24 \Omega(I_{2\Omega})}{24 \Omega + 12 \Omega} = \frac{2}{3} \text{ A}$$

$$P_{10\Omega} = (I_{10\Omega})^2 10 \Omega = \left( \frac{2}{3} \text{ A} \right)^2 \cdot 10 \Omega = 4.44 \text{ W}$$

29. a.  $E = (40 \text{ mA})(1.6 \text{ k}\Omega) = 64 \text{ V}$

b.  $R_{L_2} = \frac{48 \text{ V}}{12 \text{ mA}} = 4 \text{ k}\Omega$

$$R_{L_3} = \frac{24 \text{ V}}{8 \text{ mA}} = 3 \text{ k}\Omega$$

c.  $I_{R_1} = 72 \text{ mA} - 40 \text{ mA} = 32 \text{ mA}$

$$I_{R_2} = 32 \text{ mA} - 12 \text{ mA} = 20 \text{ mA}$$

$$I_{R_3} = 20 \text{ mA} - 8 \text{ mA} = 12 \text{ mA}$$

$$R_1 = \frac{V_{R_1}}{I_{R_1}} = \frac{64 \text{ V} - 48 \text{ V}}{32 \text{ mA}} = \frac{16 \text{ V}}{32 \text{ mA}} = 0.5 \text{ k}\Omega$$

$$R_2 = \frac{V_{R_2}}{I_{R_2}} = \frac{48 \text{ V} - 24 \text{ V}}{20 \text{ mA}} = \frac{24 \text{ V}}{20 \text{ mA}} = 1.2 \text{ k}\Omega$$

$$R_3 = \frac{V_{R_3}}{I_{R_3}} = \frac{24 \text{ V}}{12 \text{ mA}} = 2 \text{ k}\Omega$$

31. a. yes

$$\text{b. VDR: } V_{R_2} = 3 \text{ V} = \frac{R_2(12 \text{ V})}{R_1 + R_2} = \frac{R_2(12 \text{ V})}{1 \text{ k}\Omega}$$

$$R_2 = \frac{3 \text{ V}(1 \text{ k}\Omega)}{12 \text{ V}} = 0.25 \text{ k}\Omega = 250 \Omega$$

$$R_1 = 1 \text{ k}\Omega - 0.25 \text{ k}\Omega = 0.75 \text{ k}\Omega = 750 \Omega$$

c.  $V_{R_1} = E - V_L = 12 \text{ V} - 3 \text{ V} = 9 \text{ V}$  (Chose  $V_{R_1}$  rather than  $V_{R_2 \parallel R_L}$  since numerator of VDR equation "cleaner")

$$V_{R_1} = 9 \text{ V} = \frac{R_1(12 \text{ V})}{R_1 + (R_2 \parallel R_L)}$$

$$9R_1 + 9(R_2 \parallel R_L) = 12R_1$$

$$\left. \begin{array}{l} R_1 = 3(R_2 \parallel R_L) \\ R_1 + R_2 = 1 \text{ k}\Omega \end{array} \right\} 2 \text{ eq. 2 unk}(R_L = 10 \text{ k}\Omega)$$

$$R_1 = \frac{3R_2R_L}{R_2 + R_L} \Rightarrow \frac{3R_2 10 \text{ k}\Omega}{R_2 + 10 \text{ k}\Omega}$$

$$\text{and } R_1(R_2 + 10 \text{ k}\Omega) = 30 \text{ k}\Omega R_2$$

$$R_1R_2 + 10 \text{ k}\Omega R_1 = 30 \text{ k}\Omega R_2$$

$$R_1 + R_2 = 1 \text{ k}\Omega: (1 \text{ k}\Omega - R_2)R_2 + 10 \text{ k}\Omega (1 \text{ k}\Omega - R_2) = 30 \text{ k}\Omega R_2$$

$$R_2^2 + 39 \text{ k}\Omega R_2 - 10 \text{ k}\Omega^2 = 0$$

$$R_2 = 0.255 \text{ k}\Omega, -39.255 \text{ k}\Omega$$

$$R_2 = 255 \Omega$$

$$R_1 = 1 \text{ k}\Omega - R_2 = 745 \Omega$$

33. a.  $I_{CS} = 1 \text{ mA}$

$$\text{b. } R_{\text{shunt}} = \frac{R_m I_{CS}}{I_{\text{max}} - I_{CS}} = \frac{(100 \Omega)(1 \text{ mA})}{20 \text{ A} - 1 \text{ mA}} \cong \frac{0.1}{20} \Omega = 5 \text{ m}\Omega$$

$$35. \text{ a. } R_s = \frac{V_{\text{max}} - V_{VS}}{I_{CS}} = \frac{15 \text{ V} - (50 \mu\text{A})(1 \text{ k}\Omega)}{50 \mu\text{A}} = 300 \text{ k}\Omega$$

$$\text{b. } \Omega/\text{V} = 1/I_{CS} = 1/50 \mu\text{A} = 20,000$$

$$37. 10 \text{ M}\Omega = (0.5 \text{ V})(\Omega/\text{V}) \Rightarrow \Omega/\text{V} = 20 \times 10^6$$

$$I_{CS} = 1/(\Omega/\text{V}) = \frac{1}{20 \times 10^6} = 0.05 \mu\text{A}$$

## CHAPTER 7 (Even)

2. a.  $R_T = 4\ \Omega + 4\ \Omega + 4\ \Omega = 12\ \Omega$   
 b.  $R_T = 4\ \Omega + 4\ \Omega \parallel 4\ \Omega = 4\ \Omega + 2\ \Omega = 6\ \Omega$   
 c.  $R_T = (4\ \Omega + 4\ \Omega) \parallel 4\ \Omega + 4\ \Omega = 8\ \Omega \parallel 4\ \Omega + 4\ \Omega$   
 $= 2.667\ \Omega + 4\ \Omega = 6.667\ \Omega$   
 d.  $R_T = 4\ \Omega$
4. a.  $R_T = R_1 \parallel R_2 + R_3 = 12\ \Omega \parallel 6\ \Omega + 12\ \Omega = 4\ \Omega + 12\ \Omega = 16\ \Omega$   
 b.  $I = \frac{E}{R_T} = \frac{64\ \text{V}}{16\ \Omega} = 4\ \text{A}$  CDR:  $I_1 = \frac{6\ \Omega(4\ \text{A})}{6\ \Omega + 12\ \Omega} = 1\frac{1}{3}\ \text{A}$   
 c.  $V_3 = IR_3 = (4\ \text{A})(12\ \Omega) = 48\ \text{V}$
6.  $I_1 = \frac{20\ \text{V}}{5\ \Omega} = 4\ \text{A}$   
 $R_T = 16\ \Omega \parallel 25\ \Omega = 9.756\ \Omega$   
 $I_2 = \frac{7\ \text{V}}{9.756\ \Omega} = 0.7175\ \text{A}$
8. a.  $R' = R_4 + R_5 = 14\ \Omega + 6\ \Omega = 20\ \Omega$   
 $R'' = R_2 \parallel R' = 20\ \Omega \parallel 20\ \Omega = 10\ \Omega$   
 $R''' = R'' + R_1 = 10\ \Omega + 10\ \Omega = 20\ \Omega$   
 $R_T = R_3 \parallel R''' = 5\ \Omega \parallel 20\ \Omega = 4\ \Omega$   
 $I_s = \frac{E}{R_T} = \frac{20\ \text{V}}{4\ \Omega} = 5\ \text{A}$   
 $I_1 = \frac{20\ \text{V}}{R_1 + R''} = \frac{20\ \text{V}}{10\ \Omega + 10\ \Omega} = \frac{20\ \text{V}}{20\ \Omega} = 1\ \text{A}$   
 $I_3 = \frac{20\ \text{V}}{5\ \Omega} = 4\ \text{A}$   
 $I_4 = \frac{I_1}{2} = (\text{since } R' = R_2) = \frac{1\ \text{A}}{2} = 0.5\ \text{A}$   
 b.  $V_a = I_3 R_3 - I_4 R_5 = (4\ \text{A})(5\ \Omega) - (0.5\ \text{A})(6\ \Omega) = 20\ \text{V} - 3\ \text{V} = 17\ \text{V}$   
 $V_{bc} = \left( \frac{I_1}{2} \right) R_2 = (0.5\ \text{A})(20\ \Omega) = 10\ \text{V}$
10. a.  $R_T = R_1 \parallel R_2 \parallel R_3 \parallel (R_6 + R_4 \parallel R_5)$   
 $= 12\ \text{k}\Omega \parallel 12\ \text{k}\Omega \parallel 3\ \text{k}\Omega \parallel (10.4\ \text{k}\Omega + 9\ \text{k}\Omega \parallel 6\ \text{k}\Omega)$   
 $= 6\ \text{k}\Omega \parallel 3\ \text{k}\Omega \parallel (10.4\ \text{k}\Omega + 3.6\ \text{k}\Omega)$   
 $= 2\ \text{k}\Omega \parallel 14\ \text{k}\Omega = 1.75\ \text{k}\Omega$

$$I = \frac{E}{R_T} = \frac{28 \text{ V}}{1.75 \text{ k}\Omega} = 16 \text{ mA}$$

$$R' = R_1 \parallel R_2 \parallel R_3 = 2 \text{ k}\Omega$$

$$R'' = R_6 + R_4 \parallel R_5 = 14 \text{ k}\Omega$$

$$I_6 = \frac{R'(I)}{R' + R''} = \frac{(2 \text{ k}\Omega)(16 \text{ mA})}{2 \text{ k}\Omega + 14 \text{ k}\Omega} = 2 \text{ mA}$$

$$\begin{aligned} \text{b. } V_1 &= E = 28 \text{ V} \\ V_5 &= I_6(R_4 \parallel R_5) = (2 \text{ mA})(3.6 \text{ k}\Omega) = 7.2 \text{ V} \end{aligned} \quad \text{c. } P = \frac{V_5^2}{R_5} = \frac{(7.2 \text{ V})^2}{6 \text{ k}\Omega} = 8.64 \text{ mW}$$

$$\begin{aligned} 12. \text{ a. } I_E &= \frac{V_E}{R_E} = \frac{2 \text{ V}}{1 \text{ k}\Omega} = 2 \text{ mA} \\ I_C &= I_E = 2 \text{ mA} \end{aligned}$$

$$\begin{aligned} \text{b. } I_B &= \frac{V_{R_B}}{R_B} = \frac{V_{CC} - (V_{BE} + V_E)}{R_B} = \frac{8 \text{ V} - (0.7 \text{ V} + 2 \text{ V})}{220 \text{ k}\Omega} \\ &= \frac{8 \text{ V} - 2.7 \text{ V}}{220 \text{ k}\Omega} = \frac{5.3 \text{ V}}{220 \text{ k}\Omega} = 24 \mu\text{A} \end{aligned}$$

$$\begin{aligned} \text{c. } V_B &= V_{BE} + V_E = 2.7 \text{ V} \\ V_C &= V_{CC} - I_C R_C = 8 \text{ V} - (2 \text{ mA})(2.2 \text{ k}\Omega) = 8 \text{ V} - 4.4 \text{ V} = 3.6 \text{ V} \end{aligned}$$

$$\begin{aligned} \text{d. } V_{CE} &= V_C - V_E = 3.6 \text{ V} - 2 \text{ V} = 1.6 \text{ V} \\ V_{BC} &= V_B - V_C = 2.7 \text{ V} - 3.6 \text{ V} = -0.9 \text{ V} \end{aligned}$$

14. a. Network redrawn:

$$\begin{aligned} 100 \Omega + 220 \Omega &= 320 \Omega \\ 400 \Omega \parallel 600 \Omega &= 240 \Omega \\ 400 \Omega \parallel 220 \Omega &= 141.94 \Omega \\ 240 \Omega + 141.94 \Omega &= 381.94 \Omega \end{aligned}$$

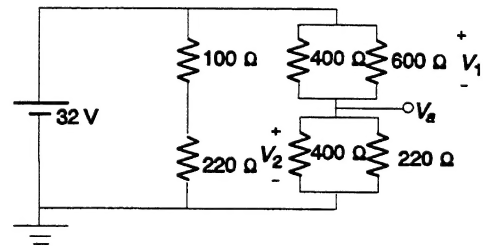
$$R_T = 320 \Omega \parallel 381.94 \Omega = 174.12 \Omega$$

$$\text{b. } V_a = \frac{141.94 \Omega (32 \text{ V})}{141.94 \Omega + 240 \Omega} = 11.892 \text{ V}$$

$$\text{c. } V_1 = 32 \text{ V} - V_a = 32 \text{ V} - 11.892 \text{ V} = 20.108 \text{ V}$$

$$\text{d. } V_2 = V_a = 11.892 \text{ V}$$

$$\begin{aligned} \text{e. } I_{600\Omega} &= \frac{20.108 \text{ V}}{600 \Omega} = 33.51 \text{ mA} \\ I_{220\Omega} &= \frac{11.892 \text{ V}}{220 \Omega} = 54.05 \text{ mA} \\ I + I_{600\Omega} &= I_{220\Omega} \\ I &= I_{220\Omega} - I_{600\Omega} \\ &= 54.05 \text{ mA} - 33.5 \text{ mA} \\ &= 20.54 \text{ mA} \rightarrow \end{aligned}$$





$$\begin{aligned}
 16. \quad R_T &= 4 \text{ k}\Omega + 2 \text{ k}\Omega \parallel (1 \text{ k}\Omega + 0.5 \text{ k}\Omega + 1.5 \text{ k}\Omega) \\
 &= 4 \text{ k}\Omega + 2 \text{ k}\Omega \parallel 3 \text{ k}\Omega = 4 \text{ k}\Omega + 1.2 \text{ k}\Omega \\
 &= 5.2 \text{ k}\Omega
 \end{aligned}$$

$$I_s = \frac{E}{R_T} = \frac{24 \text{ V}}{5.2 \text{ k}\Omega} = 4.615 \text{ mA}$$

$$I = \frac{3 \text{ k}\Omega(I_s)}{3 \text{ k}\Omega + 2 \text{ k}\Omega} = \frac{3 \text{ k}\Omega(4.615 \text{ mA})}{5 \text{ k}\Omega} = 2.769 \text{ mA}$$

$$I_{R_3} = 4.615 \text{ mA} - 2.769 \text{ mA} = 1.846 \text{ mA}$$

$$V_b = -I_{R_3}R_3 = -(1.846 \text{ mA})(1 \text{ k}\Omega) = -1.846 \text{ V}$$

$$V_a + 24 \text{ V} - I_s 4 \text{ k}\Omega = 0$$

$$\begin{aligned}
 V_a &= I_s 4 \text{ k}\Omega - 24 \text{ V} = (4.615 \text{ mA})(4 \text{ k}\Omega) - 24 \text{ V} \\
 &= 18.46 \text{ V} - 24 \text{ V} = -5.54 \text{ V}
 \end{aligned}$$

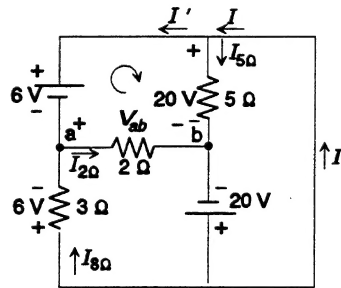
$$V_{ab} = V_a - V_b = -5.54 \text{ V} - (-1.846 \text{ V}) = -3.694 \text{ V}$$

$$18. \quad 8 \Omega \parallel 8 \Omega = 4 \Omega$$

$$I = \frac{30 \text{ V}}{4 \Omega + 6 \Omega} = \frac{30 \text{ V}}{10 \Omega} = 3 \text{ A}$$

$$V = I(8 \Omega \parallel 8 \Omega) = (3 \text{ A})(4 \Omega) = 12 \text{ V}$$

20. a.



$$\begin{aligned}
 \text{KVL: } +6 \text{ V} - 20 \text{ V} + V_{ab} &= 0 \\
 V_{ab} &= +20 \text{ V} - 6 \text{ V} = 14 \text{ V}
 \end{aligned}$$

$$b. \quad I_{5\Omega} = \frac{20 \text{ V}}{5 \Omega} = 4 \text{ A}$$

$$I_{2\Omega} = \frac{V_{ab}}{2 \Omega} = \frac{14 \text{ V}}{2 \Omega} = 7 \text{ A}$$

$$I_{3\Omega} = \frac{6 \text{ V}}{3 \Omega} = 2 \text{ A}$$

$$I' + I_{3\Omega} = I_{2\Omega}$$

$$\text{and } I' = I_{2\Omega} - I_{3\Omega} = 7 \text{ A} - 2 \text{ A} = 5 \text{ A}$$

$$I = I' + I_{5\Omega} = 5 \text{ A} + 4 \text{ A} = 9 \text{ A}$$

$$22. \quad I_2 R_2 = 2R_3 \Rightarrow I_2 = \frac{R_3}{10} \quad (\text{since the voltage across parallel elements is the same})$$

$$I_1 = I_2 + I_3 = \frac{R_3}{10} + 2$$

$$\begin{aligned}
 \text{KVL: } 120 &= I_1 12 + I_3 R_3 = \left[ \frac{R_3}{10} + 2 \right] 12 + 2R_3 \\
 \text{and } R_3 &= 30 \Omega
 \end{aligned}$$

24.  $36 \text{ k}\Omega \parallel 6 \text{ k}\Omega \parallel 12 \text{ k}\Omega = 3.6 \text{ k}\Omega$   
 $V = \frac{3.6 \text{ k}\Omega(45 \text{ V})}{3.6 \text{ k}\Omega + 6 \text{ k}\Omega} = 16.875 \text{ V} \neq 27 \text{ V}$ . Therefore, not operating properly!  
 6 k $\Omega$  resistor "open"  
 $V = \frac{9 \text{ k}\Omega(45 \text{ V})}{9 \text{ k}\Omega + 6 \text{ k}\Omega} = 27 \text{ V}$
26. a.  $R'_T = R_4 \parallel (R_6 + R_7 + R_8) = 2 \Omega \parallel 7 \Omega = 1.556 \Omega$   
 $R''_T = R_2 \parallel (R_3 + R_5 + R'_T) = 2 \Omega \parallel (4 \Omega + 1 \Omega + 1.556 \Omega) = 1.532 \Omega$   
 $R_T = R_1 + R''_T = 4 \Omega + 1.532 \Omega = 5.532 \Omega$
- b.  $I = 2 \text{ V}/5.532 \Omega = 0.3615 \text{ A} = 361.5 \text{ mA}$
- c.  $I_3 = \frac{2 \Omega(I)}{2 \Omega + 6.56 \Omega} = \frac{2 \Omega(361.5 \text{ mA})}{2 \Omega + 6.56 \Omega} = 84.5 \text{ mA}$   
 $I_8 = \frac{2 \Omega(84.5 \text{ mA})}{2 \Omega + 7 \Omega} = 18.78 \text{ mA}$
28. a.  $R_{10} + R_{11} \parallel R_{12} = 1 \Omega + 2 \Omega \parallel 2 \Omega = 2 \Omega$   
 $R_4 \parallel (R_5 + R_6) = 10 \Omega \parallel 10 \Omega = 5 \Omega$   
 $R_1 + R_2 \parallel (R_3 + 5 \Omega) = 3 \Omega + 6 \Omega \parallel 6 \Omega = 6 \Omega$   
 $R_T = 2 \Omega \parallel 3 \Omega \parallel 6 \Omega = 2 \Omega \parallel 2 \Omega = 1 \Omega$   
 $I = 12 \text{ V}/1 \Omega = 12 \text{ A}$
- b.  $I_1 = 12 \text{ V}/6 \Omega = 2 \text{ A}$   
 $I_3 = \frac{6 \Omega(2 \text{ A})}{6 \Omega + 6 \Omega} = 1 \text{ A}$   
 $I_4 = \frac{1 \text{ A}}{2} = 0.5 \text{ A}$
- c.  $I_6 = I_4 = 0.5 \text{ A}$
- d.  $I_{10} = \frac{12 \text{ A}}{2} = 6 \text{ A}$
30.  $I_{R_1} = 40 \text{ mA}$   
 $I_{R_2} = 40 \text{ mA} - 10 \text{ mA} = 30 \text{ mA}$   
 $I_{R_3} = 30 \text{ mA} - 20 \text{ mA} = 10 \text{ mA}$   
 $I_{R_5} = 40 \text{ mA}$   
 $I_{R_4} = 40 \text{ mA} - 4 \text{ mA} = 36 \text{ mA}$   
 $R_1 = \frac{V_{R_1}}{I_{R_1}} = \frac{120 \text{ V} - 100 \text{ V}}{40 \text{ mA}} = \frac{20 \text{ V}}{40 \text{ mA}} = 0.5 \text{ k}\Omega$   
 $R_2 = \frac{V_{R_2}}{I_{R_2}} = \frac{100 \text{ V} - 40 \text{ V}}{30 \text{ mA}} = \frac{60 \text{ V}}{30 \text{ mA}} = 2 \text{ k}\Omega$   
 $R_3 = \frac{V_{R_3}}{I_{R_3}} = \frac{40 \text{ V}}{10 \text{ mA}} = 4 \text{ k}\Omega$   
 $R_4 = \frac{V_{R_4}}{I_{R_4}} = \frac{36 \text{ V}}{36 \text{ mA}} = 1 \text{ k}\Omega$

$$R_5 = \frac{V_{R_5}}{I_{R_5}} = \frac{60 \text{ V} - 36 \text{ V}}{40 \text{ mA}} = \frac{24 \text{ V}}{40 \text{ mA}} = 0.6 \text{ k}\Omega$$

$$P_1 = I_1^2 R_1 = (40 \text{ mA})^2 0.5 \text{ k}\Omega = 0.8 \text{ W (1 watt resistor)}$$

$$P_2 = I_2^2 R_2 = (30 \text{ mA})^2 2 \text{ k}\Omega = 1.8 \text{ W (2 watt resistor)}$$

$$P_3 = I_3^2 R_3 = (10 \text{ mA})^2 4 \text{ k}\Omega = 0.4 \text{ W (1/2 watt or 1 watt resistor)}$$

$$P_4 = I_4^2 R_4 = (36 \text{ mA})^2 1 \text{ k}\Omega = 1.296 \text{ W (2 watt resistor)}$$

$$P_5 = I_5^2 R_5 = (40 \text{ mA})^2 0.6 \text{ k}\Omega = 0.96 \text{ W (1 watt resistor)}$$

All power levels less than 2 W. Four less than 1 W.

$$32. \quad a. \quad V_{ab} = \frac{80 \Omega (40 \text{ V})}{100 \Omega} = 32 \text{ V}$$

$$V_{bc} = 40 \text{ V} - 32 \text{ V} = 8 \text{ V}$$

$$b. \quad 80 \Omega \parallel 1 \text{ k}\Omega = 74.07 \Omega$$

$$20 \Omega \parallel 10 \text{ k}\Omega = 19.96 \Omega$$

$$V_{ab} = \frac{74.07 \Omega (40 \text{ V})}{74.07 \Omega + 19.96 \Omega} = 31.51 \text{ V}$$

$$V_{bc} = 40 \text{ V} - 31.51 \text{ V} = 8.49 \text{ V}$$

$$c. \quad P = \frac{(31.51 \text{ V})^2}{80 \Omega} + \frac{(8.49 \text{ V})^2}{20 \Omega} = 12.411 \text{ W} + 3.604 \text{ W} = 16.015 \text{ W}$$

$$d. \quad P = \frac{(32 \text{ V})^2}{80 \Omega} + \frac{(8 \text{ V})^2}{20 \Omega} = 12.8 \text{ W} + 3.2 \text{ W} = 16 \text{ W}$$

$$34. \quad 25 \text{ mA: } R_{\text{shunt}} = \frac{(1 \text{ k}\Omega)(50 \mu\text{A})}{25 \text{ mA} - 0.05 \text{ mA}} \cong 2 \Omega$$

$$50 \text{ mA: } R_{\text{shunt}} = \frac{(1 \text{ k}\Omega)(50 \mu\text{A})}{50 \text{ mA} - 0.05 \text{ mA}} = 1 \Omega$$

$$100 \text{ mA: } R_{\text{shunt}} \cong 0.5 \Omega$$

$$36. \quad 5 \text{ V: } R_s = \frac{5 \text{ V} - (1 \text{ mA})(100 \Omega)}{1 \text{ mA}} = 4.9 \text{ k}\Omega$$

$$50 \text{ V: } R_s = \frac{50 \text{ V} - 0.1 \text{ V}}{1 \text{ mA}} = 49.9 \text{ k}\Omega$$

$$500 \text{ V: } R_s = \frac{500 \text{ V} - 0.1 \text{ V}}{1 \text{ mA}} = 499.9 \text{ k}\Omega$$

$$38. \quad a. \quad R_s = \frac{E}{I_m} - R_m - \frac{\text{zero adjust}}{2} = \frac{3 \text{ V}}{100 \mu\text{A}} - 1 \text{ k}\Omega - \frac{2 \text{ k}\Omega}{2} = 28 \text{ k}\Omega$$

$$\begin{aligned}
 \text{b. } xI_m &= \frac{E}{R_{\text{series}}} + R_m + \frac{\text{zero adjust}}{2} + R_{\text{unk}} \\
 R_{\text{unk}} &= \frac{E}{xI_m} - \left[ R_{\text{series}} + R_m + \frac{\text{zero adjust}}{2} \right] \\
 &= \frac{3 \text{ V}}{x100 \mu\text{A}} - 30 \text{ k}\Omega \Rightarrow \frac{30 \times 10^3}{x} - 30 \times 10^3 \\
 x = \frac{3}{4}, R_{\text{unk}} &= 10 \text{ k}\Omega; x = \frac{1}{2}, R_{\text{unk}} = 30 \text{ k}\Omega; x = \frac{1}{4}, R_{\text{unk}} = 90 \text{ k}\Omega
 \end{aligned}$$

40. a. Carefully redrawing the network will reveal that all three resistors are in parallel and  $R_T = \frac{R}{N} = \frac{12 \Omega}{3} = 4 \Omega$

b. Again, all three resistors are in parallel and  $R_T = \frac{R}{N} = \frac{18 \Omega}{3} = 6 \Omega$